

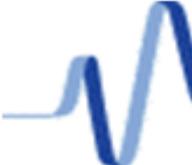
# Spectroscopie 1S-3S de l'atome d'hydrogène en vue de la détermination de constantes fondamentales et du rayon du proton

Hélène Fleurbaey, Sandrine Galtier,  
Simon Thomas, François Biraben,  
Lucile Julien et François Nez

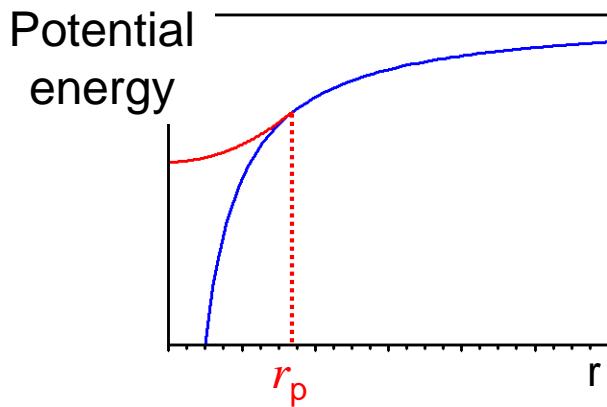
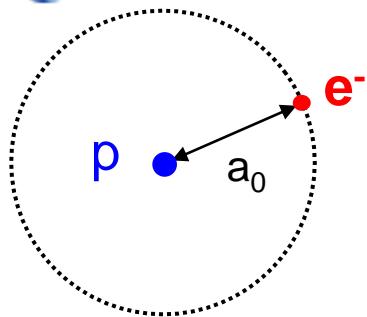
Laboratoire Kastler Brossel

Assemblée générale du Labex FIRST-TF

8-9 juin 2017



# Hydrogen theory



$$E = hcR_\infty f(\alpha, \frac{m_e}{m_p}, n, l, j) + L_n(n, l, j, r_p)$$

- Dirac equation
- recoil effect

exact

not well known

- QED corrections ( $1/n^3$ )
- proton charge radius ( $m_r^3 r_p^2/n^3$ )

- Unknown quantities :  $R_\infty$  and  $L_n$
- ➡ linear combinations of exp. data

MPQ Garching  
 LKB Paris  
 S. Karshenboim / K. Pachucki

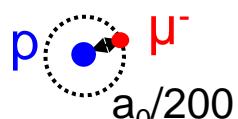
$$\left. \begin{aligned} n(1S - 2S) &= \left(1 - \frac{1}{4}\right)R_\infty + L(1S) - L(2S) \\ n(2S - 8S) &= \left(\frac{1}{4} - \frac{1}{64}\right)R_\infty + L(2S) - L(8S) \\ L(1S) - 8L(2S) &= \text{precisely calculated} \end{aligned} \right\} \begin{array}{l} R_\infty, L^{\text{exp}}(1S) \\ + \text{QED} \\ \rightarrow r_p \end{array}$$

Actually, least squares adjustment of all data available (CODATA)



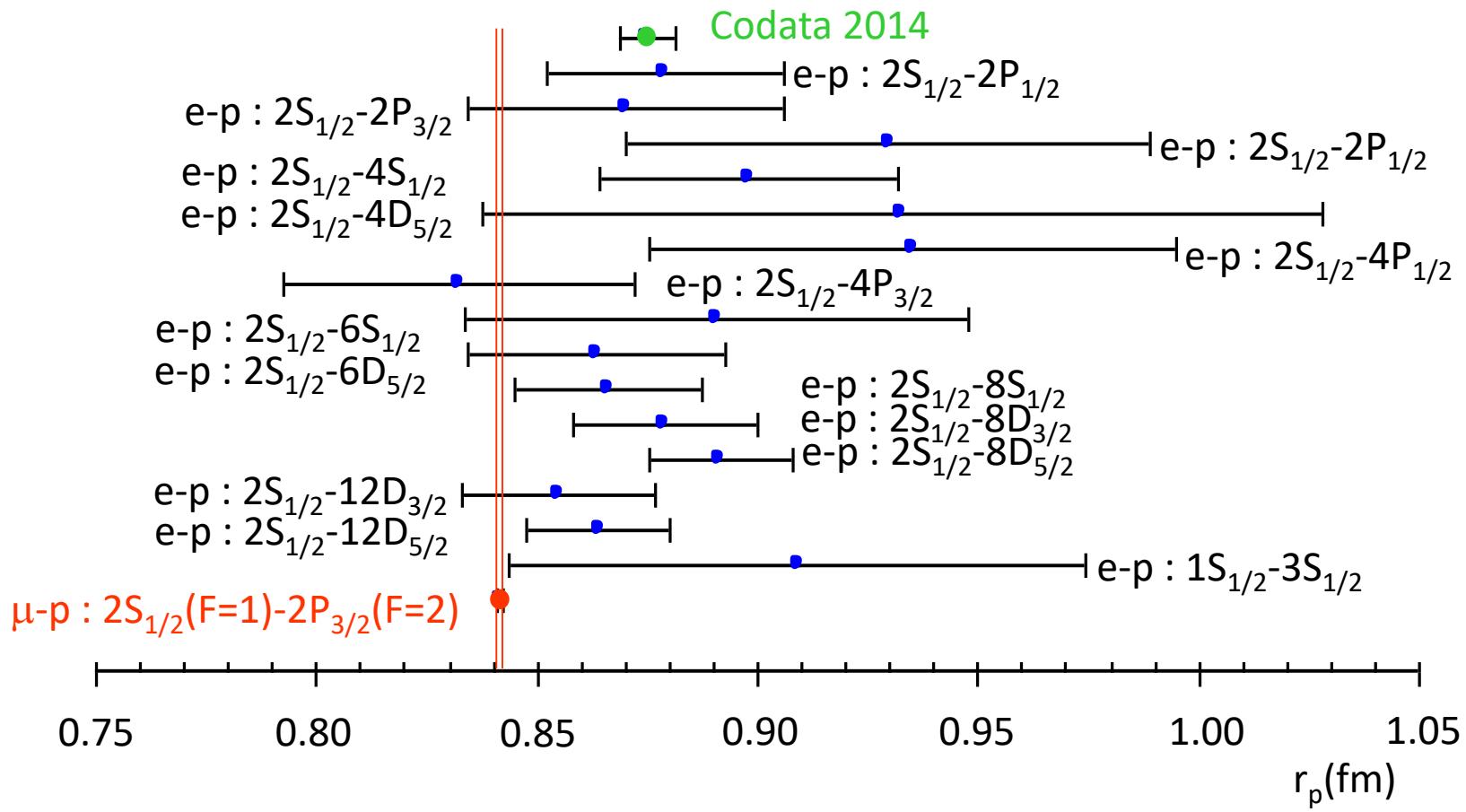
# The « proton radius puzzle »

- 2S-2P in muonic hydrogen  $\mu\text{-p}$  (Paul Scherrer Institute)



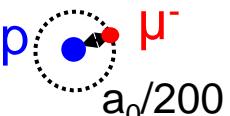
- $m_\mu \sim 200 m_e \rightarrow \Delta E_\mu(r_p) \sim 10^7 \Delta E_e(r_p)$  : 2% of  $v_{2S-2P}(\mu\text{-p})$

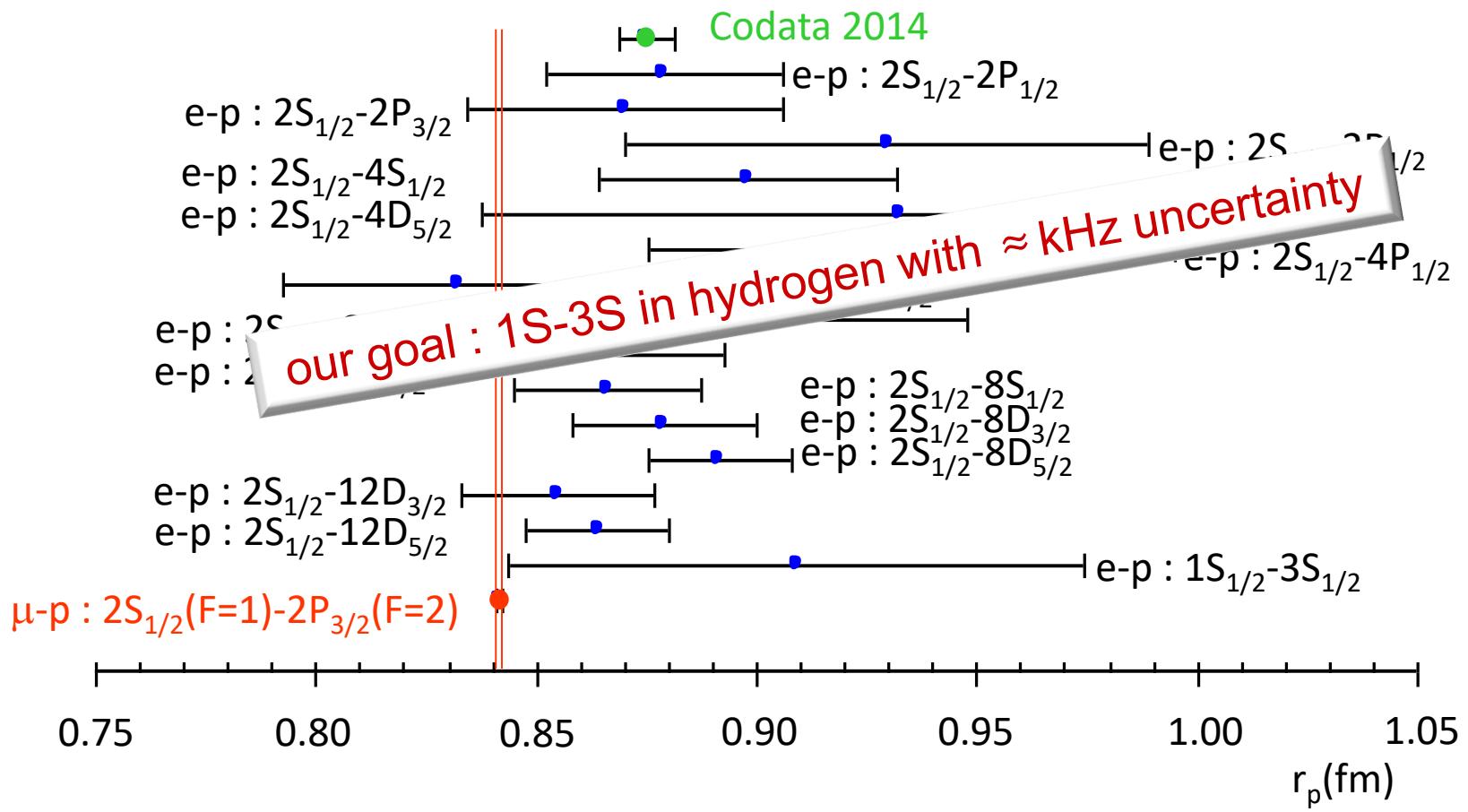
$\rightarrow$  more precise  $r_p$ , but smaller !





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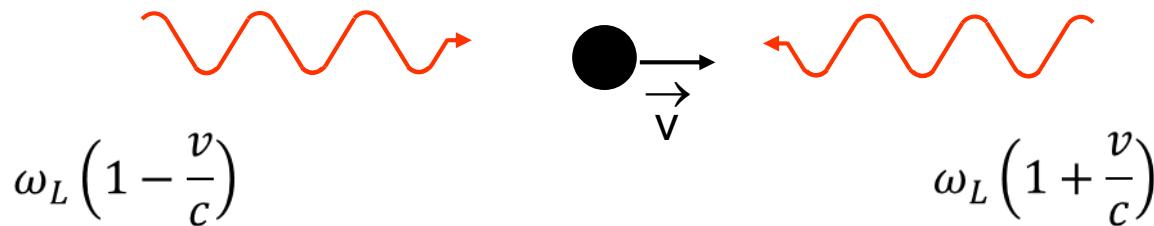
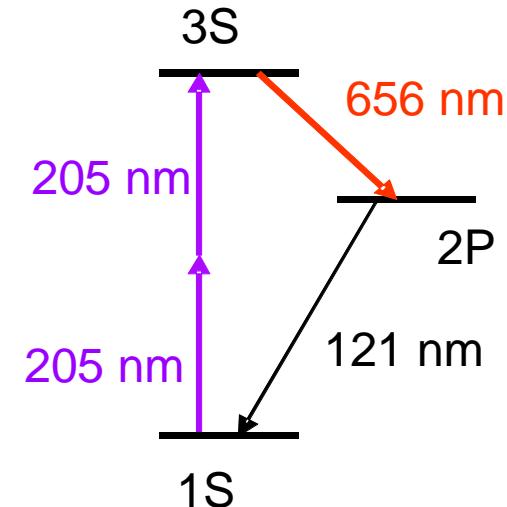
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→ more precise  $r_p$ , but smaller !





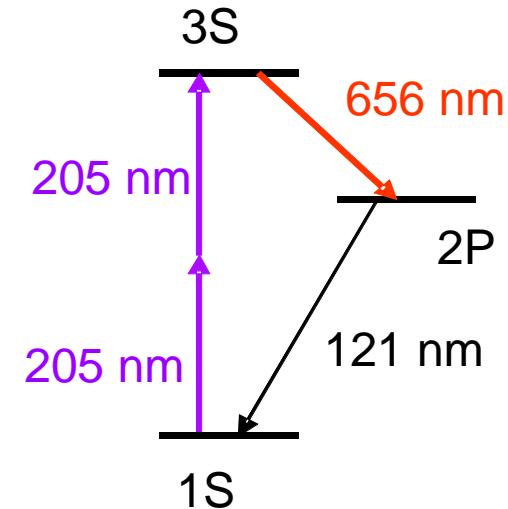
# 1S-3S spectroscopy

- Two-photon transition  
➡ No first order Doppler effect



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- 2<sup>nd</sup> order Doppler effect



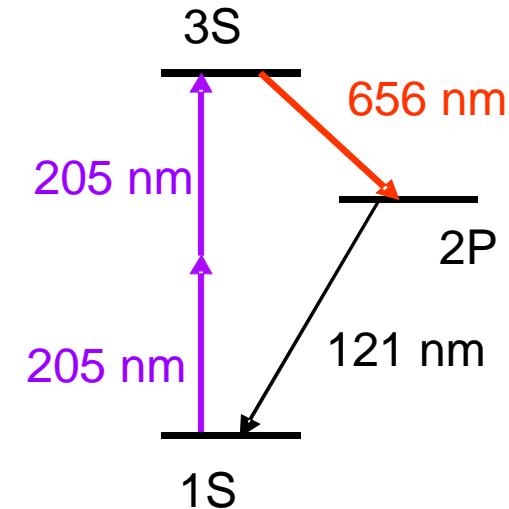
A diagram showing a particle moving to the right with velocity  $\vec{v}$ . A red wave is emitted to the right with frequency  $\omega_L \left( 1 - \frac{v}{c} + \frac{v^2}{2c^2} \right)$ . Another red wave is emitted to the left with frequency  $\omega_L \left( 1 + \frac{v}{c} + \frac{v^2}{2c^2} \right)$ .

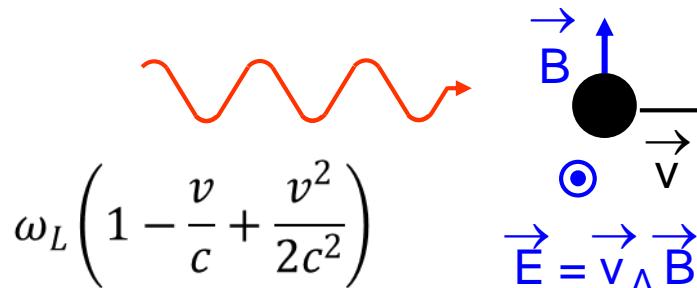
$$\delta_{Doppler} \approx -\frac{\omega_0 v^2}{2c^2}$$



# 1S-3S spectroscopy

- Two-photon transition  
➡ No first order Doppler effect
- 2<sup>nd</sup> order Doppler effect
  - No easy one-photon transition from 1S
  - ➡ Compensation with quadratic Stark effect





$$\omega_L \left( 1 - \frac{v}{c} + \frac{v^2}{2c^2} \right)$$

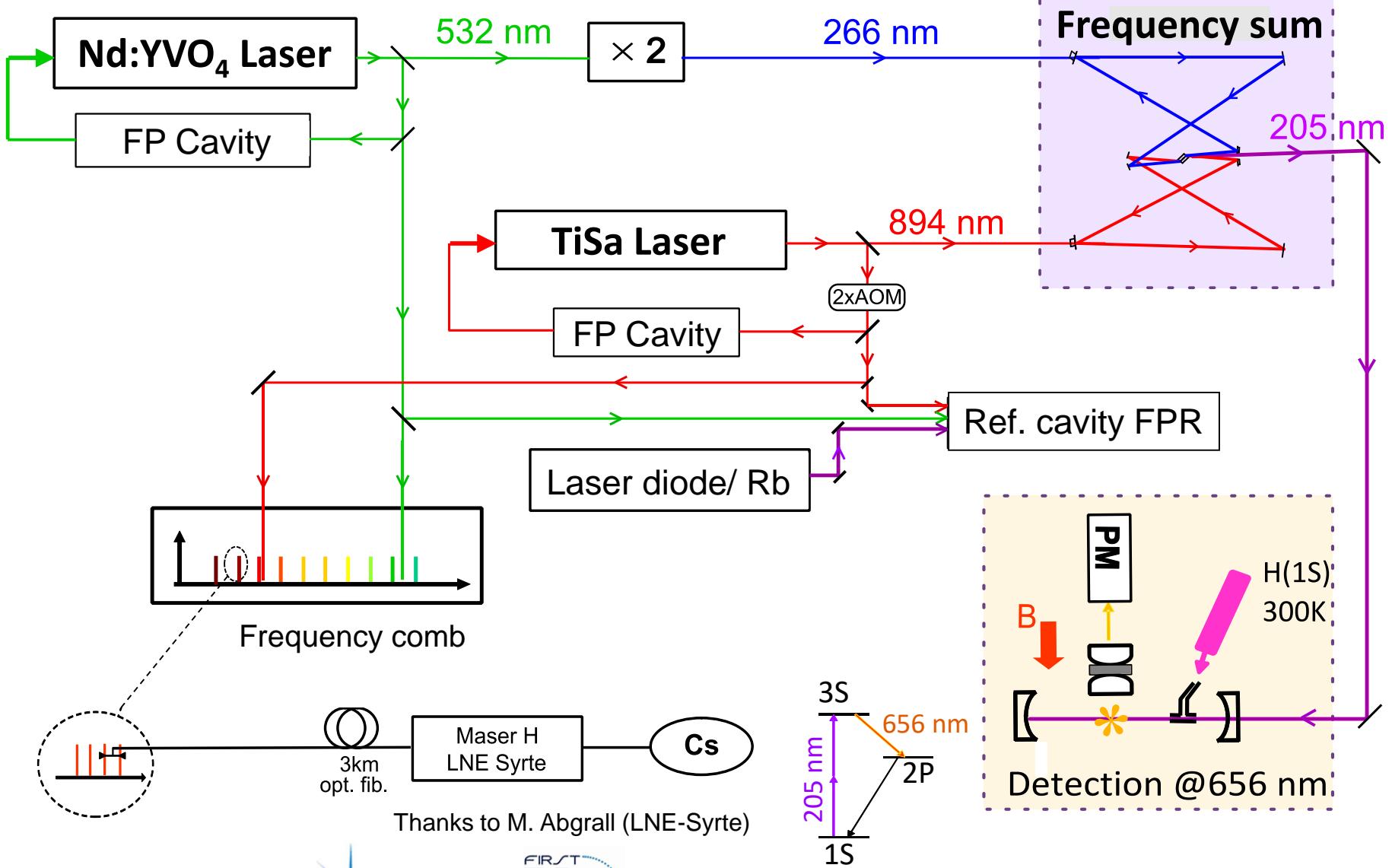
$$\omega_L \left( 1 + \frac{v}{c} + \frac{v^2}{2c^2} \right)$$

$$\vec{E} = \vec{v} \wedge \vec{B}$$

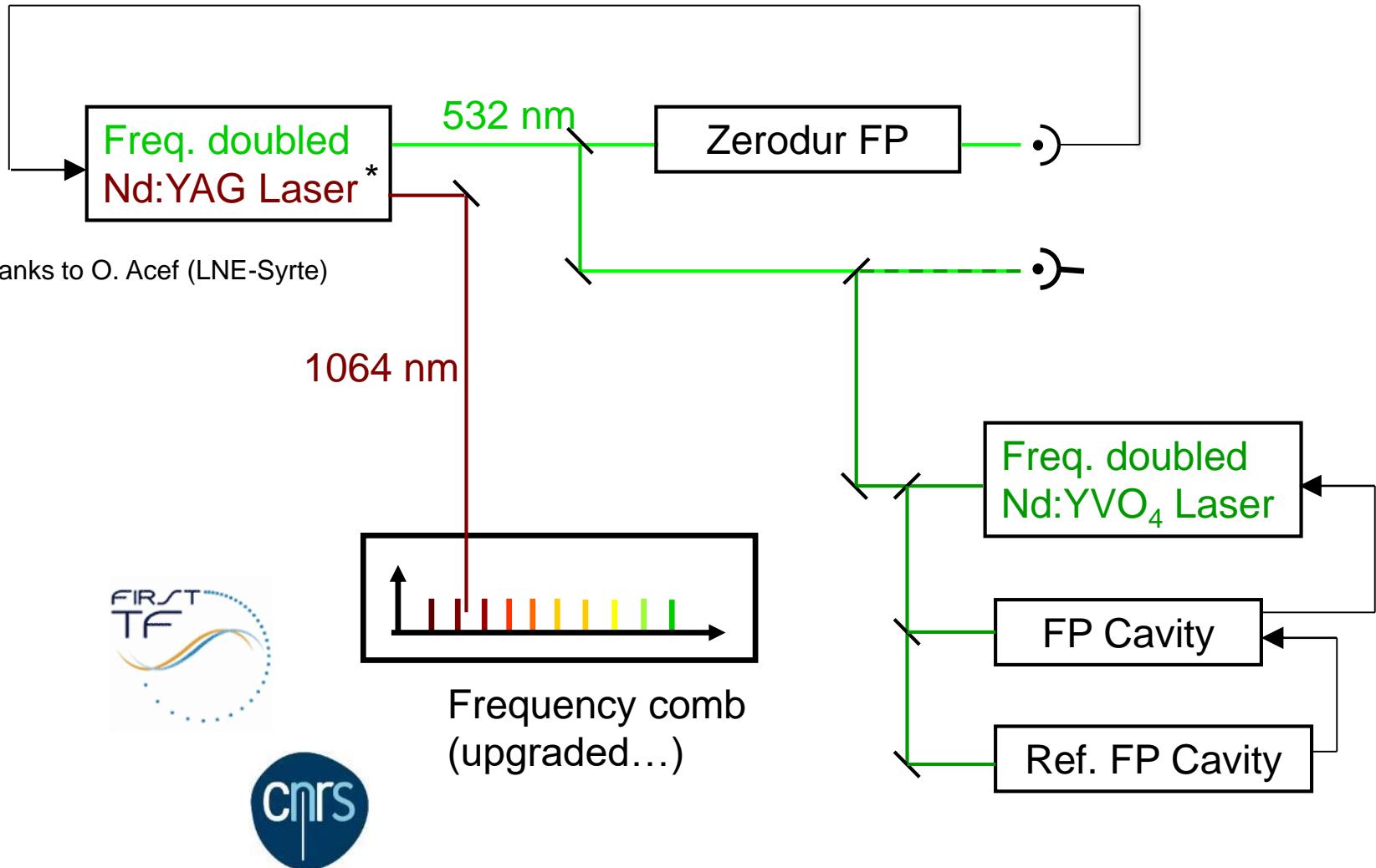
$$\delta_{Doppler} \approx -\frac{\omega_0 v^2}{2c^2} \quad \leftrightarrow \quad \delta_{Stark} \propto \frac{v^2 B^2}{\Delta\nu_{SP}}$$

- In practice: only partial compensation
  - Fit for various B values ➡ velocity distribution estimation

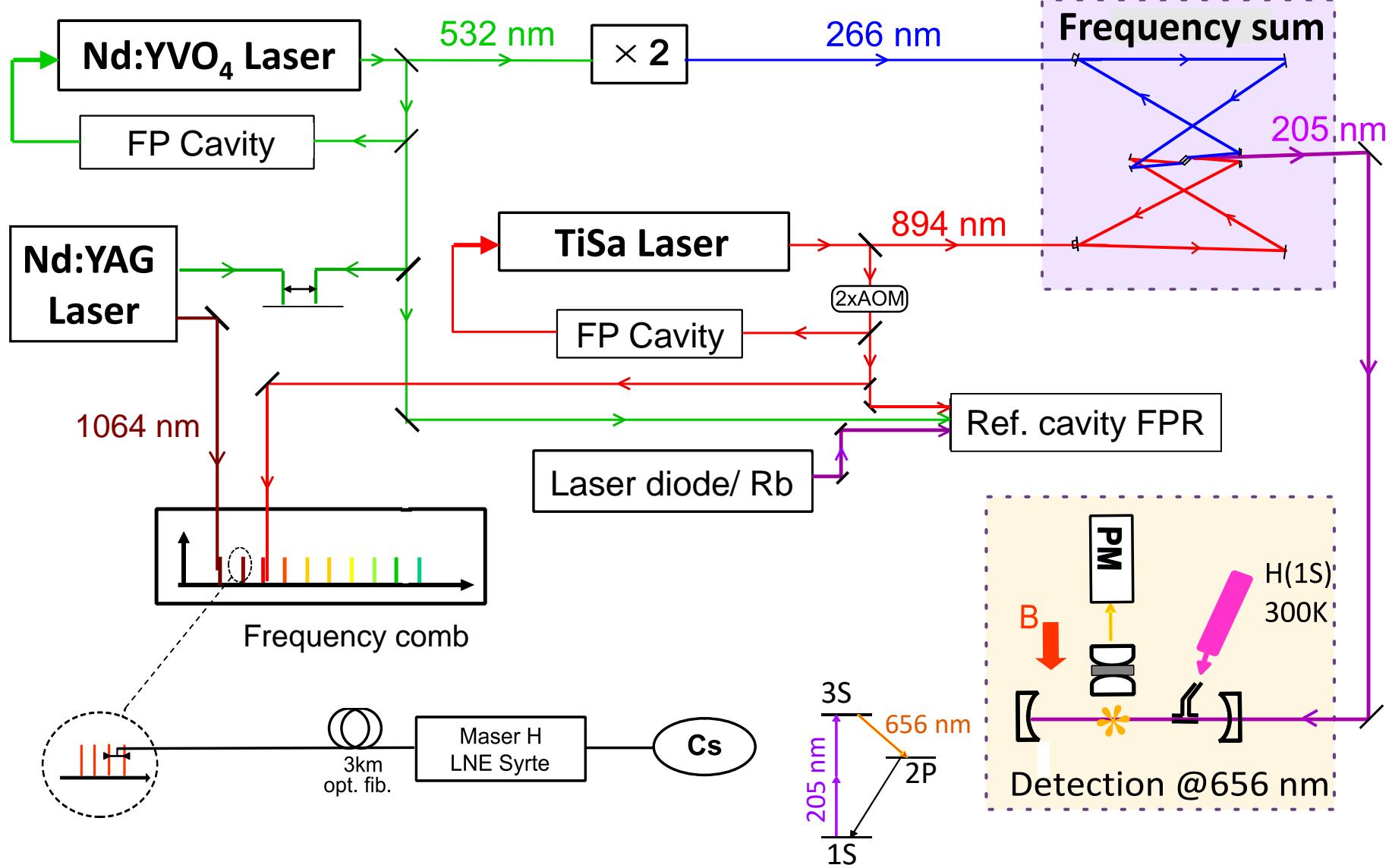
# Experimental setup



# Improving the 532 nm frequency measurement



# Experimental setup : update





# Data analysis

## → Data acquisition:

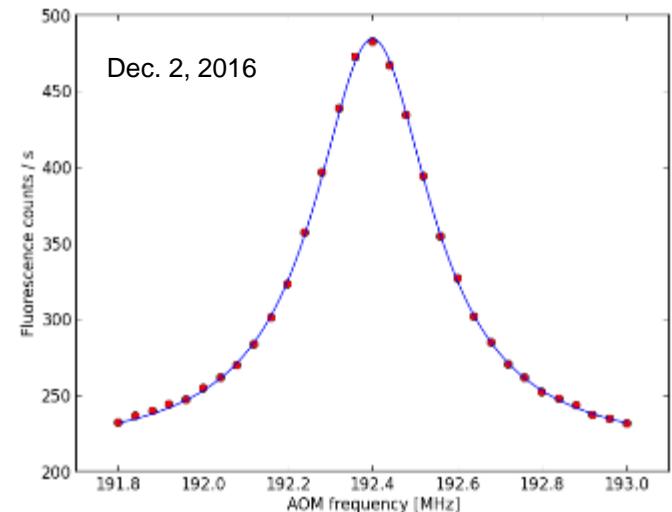
- frequency  $f_{1S-3S} = 2(2 \times f_{verdi}^{FPR} + (f_{tisa}^{FPR} - 2 \times f_{AOM}))$
- fluorescence
- UV intensity, ...
- for several B field values
  - and 3 different pressures

## → Analysis:

- fit with theoretical profile
- estimate velocity distribution

## → Systematic effects:

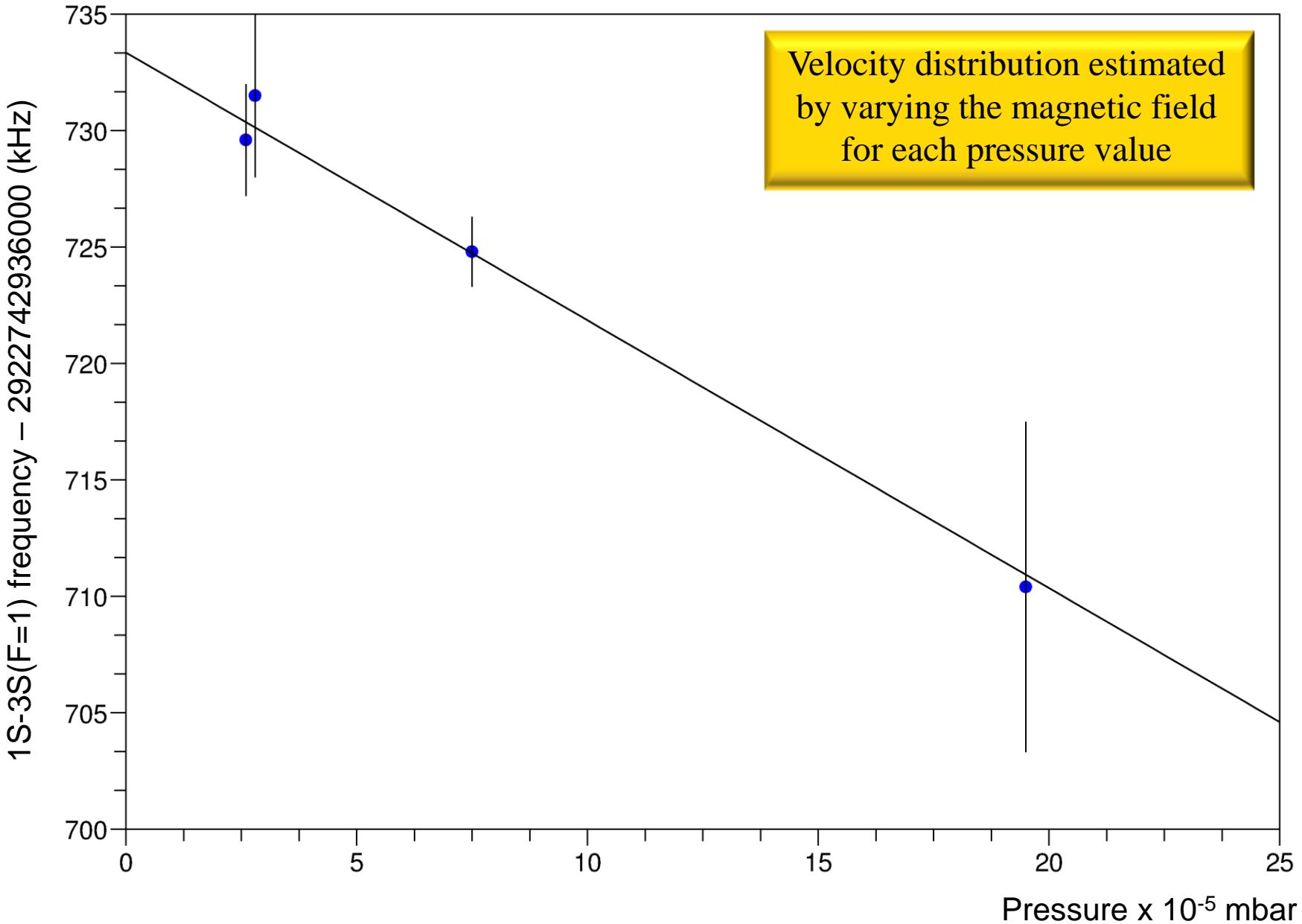
- pressure shift
- light shift
- quantum interference



Integration time : 4h  
 $P_{205} = 6.5 \text{ mW}$   
Pressure =  $3 \times 10^{-5} \text{ mbar}$   
 $B = -0.3 \text{ G}$



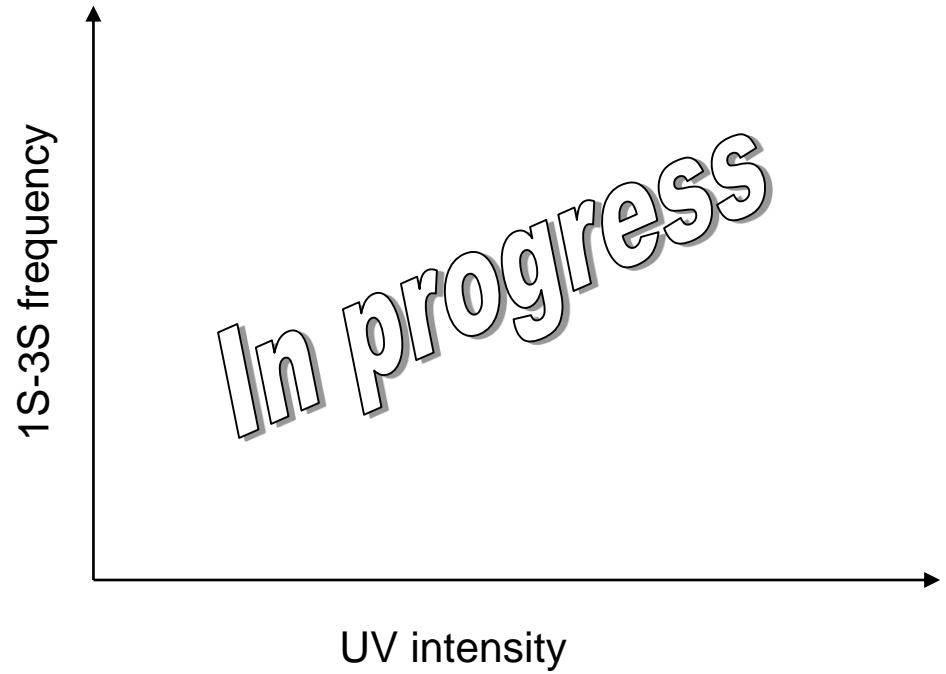
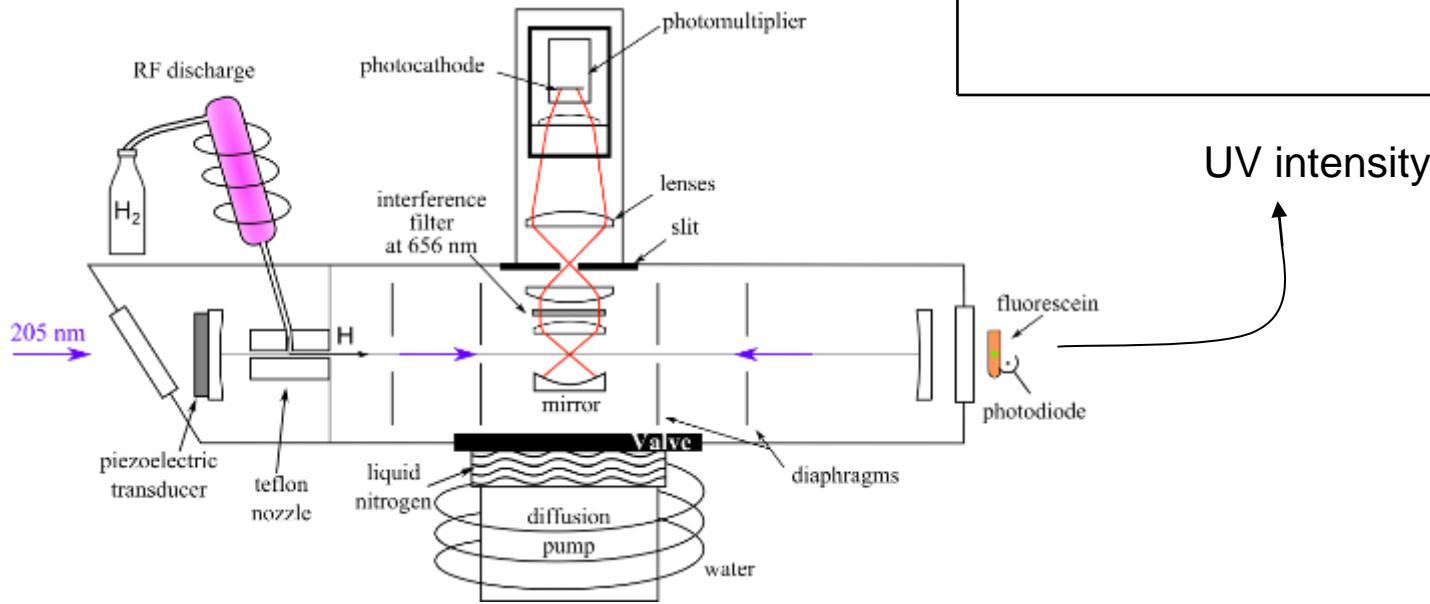
# Pressure shift





# Light shift

- Large effect (several kHz)
- Hard to measure
- Monitor the UV power
  - Photodiodes with fluorescein
- Analysis in progress



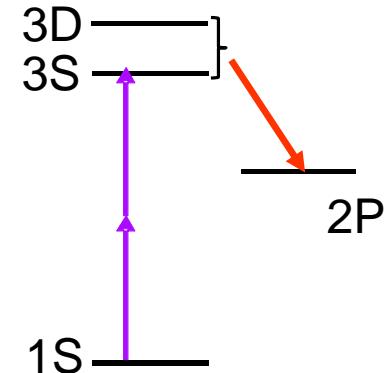
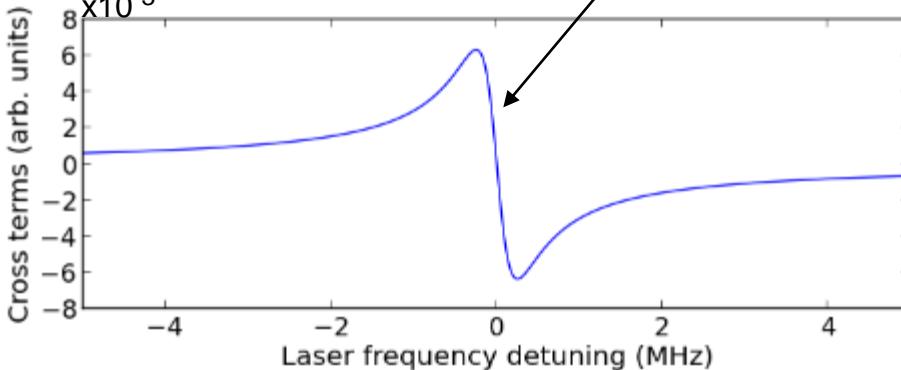
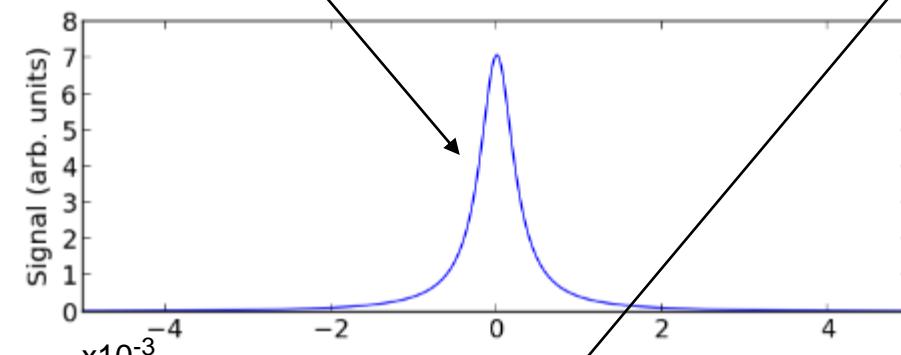


# Quantum interference

- Same initial and final state  
➡ Interference between different paths

- Coherent sum

$$\begin{aligned} \Rightarrow P &= |A_{3S} + A_{3D}|^2 \\ &= |A_{3S}|^2 + |A_{3D}|^2 + \underbrace{A_{3S} A_{3D}^*}_{\text{c.c.}} + c.c. \end{aligned}$$



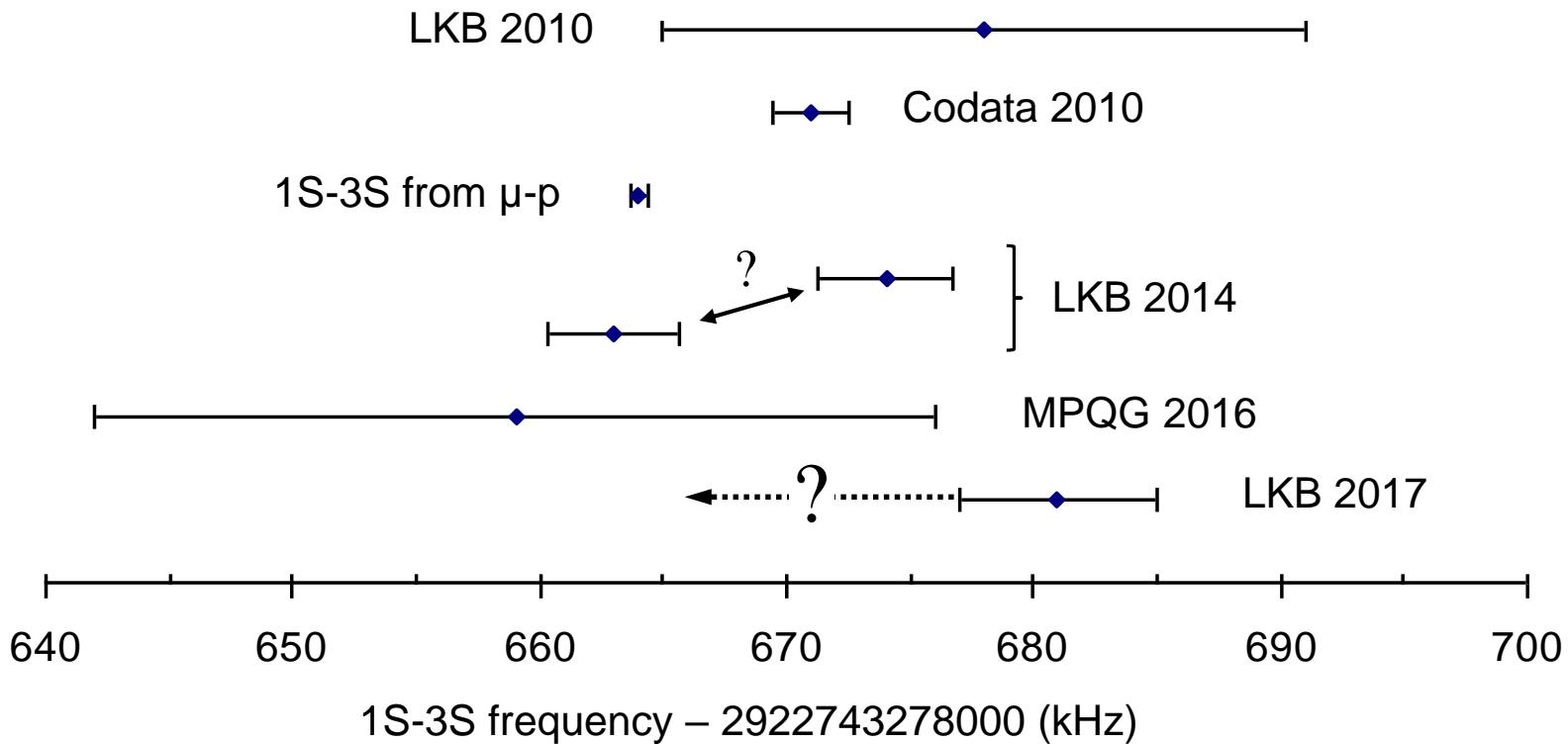
$\Gamma_{3S} = 1 \text{ MHz}$   
 $\Delta\nu_{3S-3D} = 3 \text{ GHz}$

- Frequency shift depends on detection geometry:
- for point-like detector:  
max shift < 1000 Hz
- integrate over detection cone:  
shift < 600 Hz



# Conclusion & perspectives

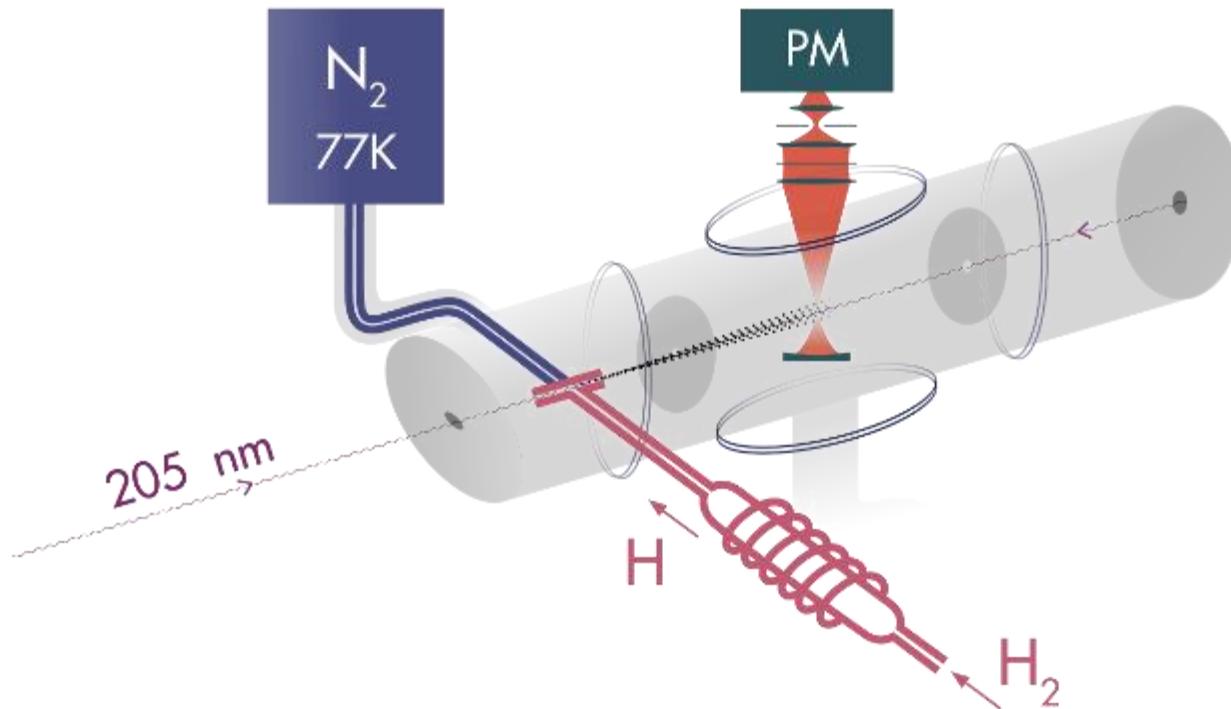
- Our goal : 1S-3S transition frequency with  $\approx$  kHz uncertainty
- Shed light on the “proton radius puzzle”





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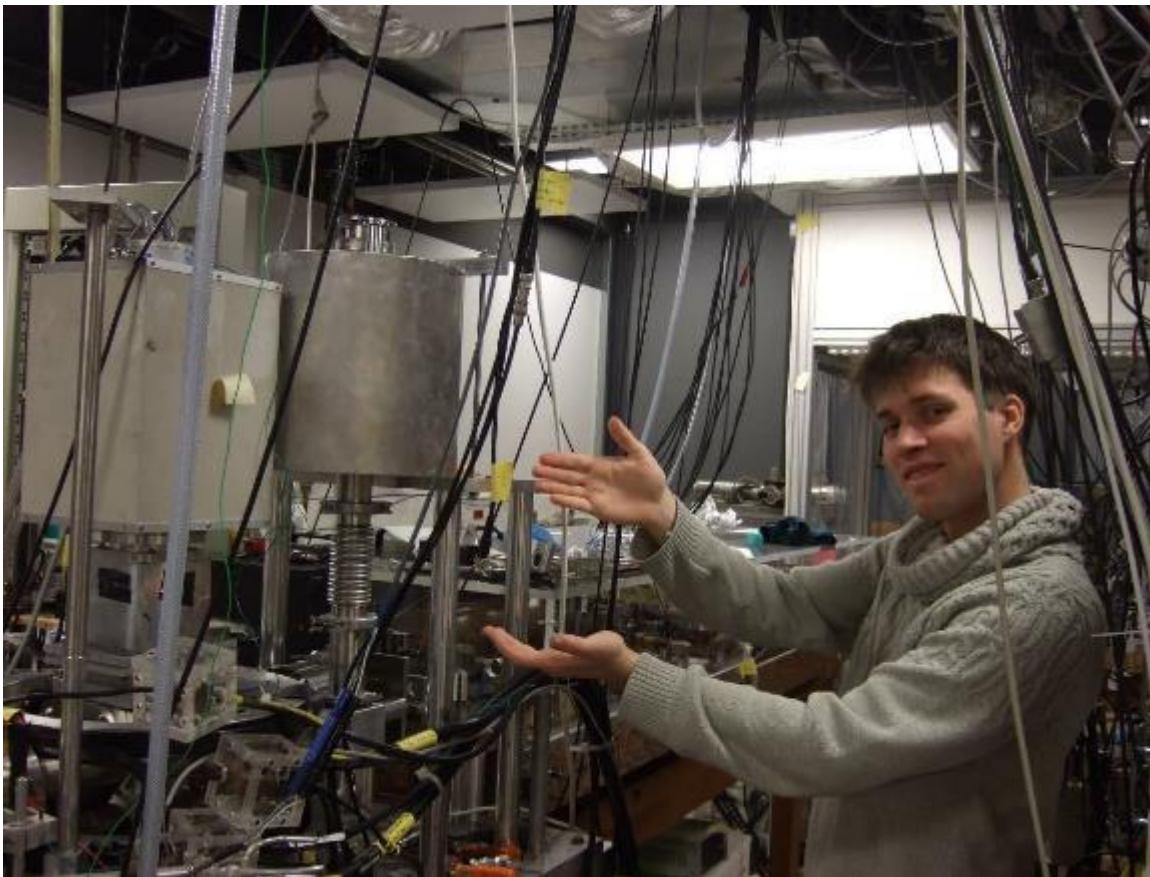
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  - In progress: cooled H atoms (77 K)





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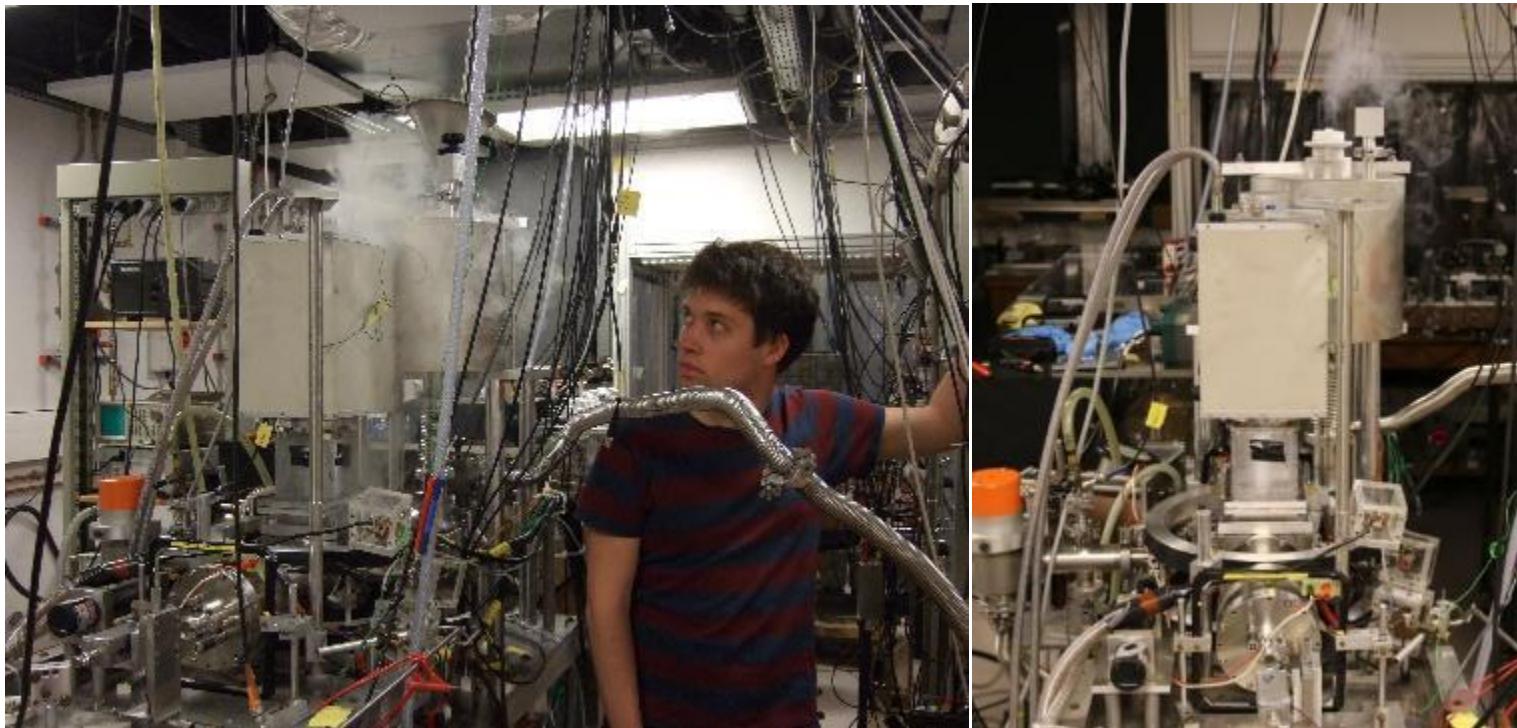
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# Conclusion & perspectives

- ➡ Our goal : 1S-3S transition frequency with  $\approx$  kHz uncertainty
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- ➡ Long-term perspective
- 1S-4S transition (194 nm)



THANK YOU



COLLÈGE  
DE FRANCE  
1530

